

**The Shafarevich conjecture of holomorphic
convexity for algebraic varieties with linear fundamental groups**

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Abstract

The Shafarevich conjecture for holomorphic convexity predicts that the universal covering space of a projective algebraic complex manifold should be holomorphically convex. The general case seems very difficult but, when the fundamental group has a faithful Zariski dense representation in a complex algebraic group G , the method of harmonic mappings can be used successfully in combination with Simpson's results on character varieties of fundamental groups of algebraic manifolds. Building on earlier work by Jost-Zuo and Katzarkov, I have completed the proof of the conjecture when G is reductive. A work in preparation with Pantev, Ramachandran and Katzarkov should settle the general case.