THE UNIVERSITY



OF HONG KONG

Institute of Mathematical Research Department of Mathematics

SPECIAL SESSION IN ALGEBRAIC GEOMETRY

November 29, 2002 (Friday)

Room 517, Meng Wah Complex, HKU

3:10 – 4:10pm

Professor Ngaiming Mok HKU

Automorphisms on moduli spaces of minimal rational curves on Fano manifolds

Tea Break

4:30 - 5:30pm

Professor Sheng-Li Tan East China Normal University, Shanghai & IMS, CUHK *Behaviour of multiple linear systems on an algebraic surface*

All are welcome

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Ngaiming Mok HKU

Automorphisms on moduli spaces of minimal rational curves on Fano manifolds

Abstract

We consider Fano manifold *X* of Picard number 1 and irreducible components *M* of the space of minimal rational curves. This includes in particular the case where *X* is a Fano hypersurface in \mathbb{P}^n of degree $\leq n - 1$ and *M* is a space of projective lines lying on *X*. It is a natural problem to understand the extent to which the geometry of *X* is captured by the geometry of *M*. In this vein, in a joint work with Jun-Muk Hwang we raise the question as to whether the canonical map $\operatorname{Aut}_o(X) \to \operatorname{Aut}_o(M)$ is an isomorphism. After providing examples showing that this may fail in general, we show that the map is indeed an isomorphism under the additional assumption that the subvariety of *M* consisiting of members passing through a general point $x \in X$ is irreducible and of dimension at least 2.

Sheng-Li Tan East China Normal University, Shanghai & IMS, CUHK

Behaviour of multiple linear systems on an algebraic surface

Abstract

I will talk about the behaviour of the map Φ_n defined by a linear system |nD| for large n, here D is an arbitrary divisor on an algebraic surface X. More precisely, we will give effective solutions to the following problems: An explicit computation of the dimension of |nD| for large n (Riemann-Roch problem). When is the linear system |nD| base point free, birationally very ample and k-very ample? When is the image of Φ_n projectively normal? We will see that the behaviour of Φ_n depends heavily on the curves C_i with $DC_i = 0$.