THE UNIVERSITY



OF HONG KONG

Institute of Mathematical Research Department of Mathematics

## **GEOMETRY SEMINAR**

## G<sub>2</sub> manifolds and G<sub>2</sub> conifolds

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## Abstract

The exceptional properties of the octonion algebra allow us to define the notion of a  $G_2$  structure on an oriented spin 7-manifold, which is a certain "nondegenerate" 3-form that induces a Riemannian metric in a nonlinear way. The manifold is called a  $G_2$  manifold if the 3-form is parallel. Such manifolds are always Ricci-flat, and are of interest in physics. More recently, however, there has been interest in  $G_2$  "conifolds", which have a finite number of isolated "cone-like" singularities. We will begin with an introduction to  $G_2$  manifolds for a general audience, paying particular attention to the similarities and differences of  $G_2$  geometry with respect to the geometries of Kähler manifolds and of 3-manifolds. Then we will define  $G_2$  conifolds, and discuss some results about them, including their desingularization and their deformation theory. If time permits, we will speculate on possible constructions of  $G_2$  conifolds.

Date: December 20, 2012 (Thursday)

Time: 3:00 – 4:00pm

Place: Room 210, Run Run Shaw Bldg., HKU

All are welcome