THE UNIVERSITY



OF HONG KONG

Institute of Mathematical Research Department of Mathematics

CONFERENCE ON NUMBER THEORY

November 29, 2012

Room 210, Run Run Shaw Building, HKU

09:55 – 10:00 Welcoming speech by Prof. Ngaiming Mok (Director of IMR, HKU)

10:00 – 10:55 Y.K. Lau, University of Hong Kong, Hong Kong

The Shifted convolution sum problem

Abstract: Shifted convolution sums arise naturally in the study of subconvexity bounds of L-functions. In this talk, we give an exposition on the background and developed methods, and explore the direction for future investigations.

Coffee Break

11:30 – 12:25 X. Ren, Shandong University, China

Asymptotic expansions of Voronoi's summation formulas for SL₃(Z) and their applications

Abstract: Let *f* be a Maass form for $SL_3(Z)$ and let $A_f(m, n)$ be its Fourier coefficients. We will talk about asymptotic expansions of Voronoi's summation formula for $A_f(m, n)$. For applications of these asymptotic formulas, we will consider smoothly weighted sums of $A_f(m, n)$ against exponential functions $e(\alpha n^\beta)$ for $\alpha \in \mathbb{R}$, $\beta \in (0, 1]$ and $X \le n \le 2X$. From these applications one can see the duality of Voronoi's summation formula for $SL_3(Z)$.

Lunch Break

15:00 – 15:55 M.A. Korolev, Steklov Mathematical Institute, Moscow

On the moments of certain trigonometric polynomials

Abstract: Suppose that $\kappa > 0$ and let

$$I_{\kappa}(T) = \int_{0}^{T} \left| \sum_{p \le x} \frac{a_p}{\sqrt{p}} \sin\left(t \log p\right) \right|^{2\kappa} dt, \quad J_{\kappa}(T) = \int_{0}^{T} \left| \sum_{p \le x} \frac{a_p}{\sqrt{p}} \cos\left(t \log p\right) \right|^{2\kappa} dt,$$

where $2 \le x \le T^{1/\kappa}$, p runs through prime numbers and a_p is the sequence of real numbers. These integrals are called as the moments of degree 2κ of polynomials

$$\sum_{p \le x} \frac{a_p}{\sqrt{p}} \sin\left(t \log p\right) \qquad \sum_{p \le x} \frac{a_p}{\sqrt{p}} \cos\left(t \log p\right)$$

It is known that in some cases there is an asymptotic formula for these moments of the following type:

$$I_{\kappa}(T), \ J_{\kappa}(T) \sim c(\kappa)T\left(\sum_{p \leq x} \frac{a_p^2}{p}\right)^{\kappa}.$$

Using some recent results of K. Soundararajan and M. Radziwill we will prove some new asymptotic expansions for the integrals $I_{\kappa}(T)$ and $J_{\kappa}(T)$ and demonstrate some applications of these formulas to the theory of the function $S(t) = \pi^{-1} \arg \zeta(\frac{1}{2} + it)$.

Coffee Break

16:30 – 17:25 I.S. Rezvyakova, Steklov Mathematical Institute, Moscow

Zeros of linear combinations of Hecke L-functions on the critical line

Abstract: Let us consider a linear combination of Hecke *L*-functions associated with the characters of the ideal class group of the imaginary quadratic field $Q(\sqrt{-D})$. In general, such linear combinations have many non-trivial zeros outside the critical line. Nevertheless, under certain natural conditions we shall show that the critical line is an exceptional set, which contains a large proportion of their non-trivial zeros.

Organizers: Yuk-Kam Lau, Kai-Man Tsang

All are welcome