

THE UNIVERSITY



OF HONG KONG

*Institute of Mathematical Research*

*Department of Mathematics*

# PROBABILITY AND INFORMATION THEORY SEMINAR

## A Monotone Sinai theorem

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### Abstract

Let  $X$  be the space of all bi-infinite sequences of nonnegative integers less than some finite  $N$ , and endow  $X$  with the shift map  $T$ , so that  $Tx(i) = x(i+1)$ . A self-map  $f$  on  $X$  is equivariant if  $f(Tx) = Tf(x)$ , and monotone if  $f(x)(i)$  is no greater than  $x(i)$ . Let  $\mu$  and  $\nu$  be product measures on  $X$ . Sinai proved that if the entropy of  $\nu$  is less than  $\mu$ , then there exists an equivariant map so that push-forward of  $\mu$  is  $\nu$ ; in joint work with Anthony Quas, we show that if we also assume that the entropy inequality is strict and  $\mu$  stochastically dominates  $\nu$ , then Sinai's theorem can be realized via a monotone map.

Date: May 5, 2014 (Monday)

Time: 11:00am – 12:00noon

Place: Room 206, Run Run Shaw Bldg., HKU

*All are welcome*