

Institute of Mathematical Research Department of Mathematics

GEOMETRY SEMINAR

Tom and Jerry — QQ-Fano 3-folds in codimension 4

Professor Miles Reid, FRS

University of Warwick

Abstract

My aim is to write down as many QQ-Fano 3-folds *X* as possible in terms of their anticanonical rings $R(X, -K_X)$. The anticanonical ring is Gorenstein, so that in codimension ≤ 3 it is given by the Hilbert-Burch or Buchsbaum-Eisenbud structure theorems, and is not much harder to work with than a hypersurface. This covers the first few hundred families of QQ-Fano 3-folds. To go further, we use the idea of Kustin-Miller unprojection ("Constructing a bigger Gorenstein ideal from a smaller one"). We have 115 candidates for the numerical types of codimension 4 Fanos that have a Type I projection to codimension 3; in each case, we can construct at least two families of topologically different QQ-Fano 3-folds by a Kustin-Miller unprojection. The two main games, called Tom and Jerry, amount to imposing algebraic conditions on 5 × 5 skew matrixes. In total, we give around 400 constructions of around 300 families of QQ-Fano 3-folds in codimension 4.

Date: November 6, 2015 (Friday)

Time: 4:00 – 5:00pm

Place: Room 210, Run Run Shaw Bldg., HKU